

1 The Simplex Solver

C, C' are conjunctions of equations;
 i, j, m are integers;
 $a_{ij}, b_i, e, d'_i, a'_i$ are constants;
 f, f', f_i are linear expressions;
 c_i, c'_i are equations;
 x_i are variables, z_i are new variables;
 $flag$ is either *true* or *false*.

```
simplex_solve( $C$ )
  let  $C$  be of the form  $c_1 \wedge \dots \wedge c_n$ 

  for each  $i \in \{1, \dots, n\}$ 
    let  $c_i$  be of the form  $b_i = \sum_{j=1}^m a_{ij}x_j$  where  $b_i \geq 0$ 
     $f_i := b_i - \sum_{j=1}^m a_{ij}x_j$ 
     $c'_i := (z_i = f_i)$ 
  endfor

   $f := \sum_{i=1}^n f_i$ 

   $\langle flag, C', f' \rangle := \text{simplex\_opt}(\wedge_{i=1}^n c'_i, f)$ 

  let  $f'$  be of the form  $e + \sum_{j=1}^n d'_j z_j + \sum_{i=1}^m a'_i x_i$ 

  if  $e \equiv 0$  then
    return true
  else return false
endif
```